

EXAM-DAY · 90-MIN REVISION CARD

Algebra — Sets, Relations & Functions, Sequences & Series

Print this · Fold it · Carry to the exam-hall gate · Revise once · Then walk in.

FORMULAS & KEY RESULTS

SET TYPES: empty \emptyset ; subset $A \subseteq B$; power set $P(A)$ has 2^n members if $|A| = n$; universal set U contains everything in context.

SET OPERATIONS: $A \cup B$ (in A or B), $A \cap B$ (in both), $A - B$ (in A not B), $A' = U - A$ (complement).

INTERVALS: $[a, b]$ closed (both ends in); (a, b) open (both ends out); $[a, b)$ and $(a, b]$ half-open. Round bracket = excluded, square = included.

INCLUSION-EXCLUSION: $|A \cup B| = |A| + |B| - |A \cap B|$; for three sets add $|A \cap B \cap C|$ back after subtracting the pair-overlaps.

CARTESIAN PRODUCT: $A \times B = \{(a, b) : a \in A, b \in B\}$; $|A \times B| = |A| \cdot |B|$; generally $A \times B \neq B \times A$ (ordered pairs).

RELATION: any subset of $A \times B$. **DOMAIN** = set of first elements; **RANGE** = set of second elements achieved.

FUNCTION: a relation where every input has EXACTLY ONE output. Types: one-one (injective), onto (surjective), into, many-one.

AP nth TERM: $a_n = a + (n - 1)d$, where a = first term, d = common difference.

AP SUM: $S_n = n/2 [2a + (n - 1)d] = n/2 (a + l)$, where l = last term.

GP nth TERM: $a_n = a \cdot r^{n-1}$, where a = first term, r = common ratio.

GP FINITE SUM: $S_n = a(r^n - 1)/(r - 1)$ for $r \neq 1$ (use $a(1 - r^n)/(1 - r)$ when $r < 1$).

GP INFINITE SUM: $S_\infty = a/(1 - r)$, valid ONLY when $|r| < 1$.

MEANS: arithmetic mean $AM = (a + b)/2$; geometric mean $GM =$

TOP 5 PYQ PATTERNS

1 GP sum — finite S_n or infinite S_∞

3 marks · 92% of years

Find a and r · finite: $S_n = a(r^n - 1)/(r - 1)$ · infinite: check $|r| < 1$ then $S_\infty = a/(1 - r)$ · recurring decimals are infinite GPs in disguise.

2 AP nth term or sum of n terms

3 marks · 85% of years

Identify a and d · term: $a_n = a + (n - 1)d$ · sum: $S_n = n/2 [2a + (n - 1)d]$ or $n/2(a + l)$.

3 Venn-diagram counting word problem

4 marks · 80% of years

Use $|A \cup B| = |A| + |B| - |A \cap B|$ · draw the two circles · fill only-A, both, only-B, neither · verify the four regions sum to the total.

4 Cartesian product / domain-range / is-it-a-function

3 marks · 78% of years

$A \times B$ = ordered pairs · domain = first elements, range = second · function test: every input exactly one output (no repeated x with different y).

5 Set type / power-set count / interval notation

2 marks · 70% of years

Power set of n elements = 2^n subsets · \in for element, \subseteq for subset · round bracket excludes, square bracket includes the endpoint.

90-MIN REVISION FLOW

0-15 min

Memorise the four series formulas (AP term + sum, GP term + sum) and the infinite-GP formula with its $|r| < 1$ condition. These five formulas are the spine of nearly half the chapter's marks.

15-35 min

Do 4 AP problems (two nth-term, two sum) and 4 GP problems (two finite-sum, two infinite-sum). Write a , d or a , r explicitly at the top of each. Speed target: 2 minutes each.

35-50 min

Drill 4 Venn-diagram counting problems. Draw the two circles every time and fill all four regions (only-A, both, only-B, neither); verify their sum to the total.

50-65 min

Practise 4 relations/functions items — write $A \times B$ for small sets, give domain and range, and decide 'function or not' with the one-output-per-input justification.

65-80 min

Sets quick-fire: power-set counts (2^n), \in versus \subseteq , and interval notation (open versus closed). Aim for 30 seconds per item.

80-90 min

Self-check — recall from memory: the GP infinite-sum formula and its condition, the inclusion-exclusion formula, the domain/range definitions, and the AP sum formula. If all four come instantly, you are chapter-ready.

\sqrt{ab} ; always $AM \geq GM$ for positive a, b .

Confidence, not anxiety. You've practised this all year. Trust your steps. Don't change strategy on exam morning.
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