

ANSWER KEY & MARKING SCHEME · CBSE CLASS 9

Polynomials

Mathematics · Chapter 2 · Use this with the Board Paper · Companion to Quick Drill

HOW TO USE

Attempt the Board Paper first (closed-book, full time). Then come here. For 2-mark+ questions, compare your answer to the model. For 3-4 mark questions, also consult the **Topper Templates** below — these show the exact step-by-step structure that scores full marks per CBSE marking-scheme conventions.

MODEL ANSWERS · BOARD PAPER

Section A — Very Short Answer

Q1. Find the degree of the polynomial $5x^4 - 3x^3 + 2x - 7$. [1 mark]

Ans: Degree = 4 (highest power of x).

Q2. Is root 2 times $x^2 + 3x + 1$ a polynomial? Justify. [1 mark]

Ans: Yes; coefficients may be irrational (here root 2) but the exponents 2, 1, 0 are non-negative integers, satisfying the polynomial definition.

Q3. Find the zero of $p(x) = 3x - 9$. [1 mark]

Ans: $3x - 9 = 0$ gives $x = 3$. Zero is 3.

Q4. Classify $x^3 + 2x$ by terms and by degree. [1 mark]

Ans: Binomial (2 terms); cubic polynomial (degree 3).

Section B — Short Answer I

Q5. Use the Remainder Theorem to find the remainder when $p(x) = x^3 - ax^2 + 6x - a$ is divided by $(x - a)$. [2 marks]

Ans: By Remainder Theorem, remainder = $p(a) = a^3 - a \text{ times } a^2 + 6a - a = a^3 - a^3 + 6a - a = 5a$.

Q6. Evaluate $(102)^3$ using a suitable identity. [2 marks]

Ans: $(100 + 2)^3 = 100^3 + 3(100)^2(2) + 3(100)(2)^2 + 2^3 = 1000000 + 60000 + 1200 + 8 = 1061208$.

Q7. Factorise: $x^2 + 7x + 12$ by splitting the middle term. [2 marks]

Ans: Need two numbers summing to 7, product 12: 3 and 4. $x^2 + 3x + 4x + 12 = x(x+3) + 4(x+3) = (x+3)(x+4)$.

Q8. Find the value of k if $(x - 2)$ is a factor of $p(x) = 2x^3 - 6x^2 + 5x + k$. [2 marks]

Ans: By Factor Theorem, $p(2) = 0$. $p(2) = 16 - 24 + 10 + k = 2 + k = 0$, so $k = -2$.

Section C — Short Answer II

Q9. Factorise: $x^3 - 23x^2 + 142x - 120$. [3 marks]

Ans: $p(1) = 1 - 23 + 142 - 120 = 0$, so $(x - 1)$ is a factor. Dividing: $x^3 - 23x^2 + 142x - 120 = (x - 1)(x^2 - 22x + 120)$. Split: $120 = 10 \text{ times } 12$ with $10 + 12 = 22$. So $x^2 - 22x + 120 = (x - 10)(x - 12)$. Final: $(x - 1)(x - 10)(x - 12)$.

Q10. If $x + y + z = 0$, show that $x^3 + y^3 + z^3 = 3xyz$. [3 marks]

Ans: Identity: $x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)$. Given $x + y + z = 0$, the right-hand side becomes 0 times anything = 0. Hence $x^3 + y^3 + z^3 - 3xyz = 0$, that is $x^3 + y^3 + z^3 = 3xyz$.

Q11. Factorise: $27x^3 + y^3 + z^3 - 9xyz$. [3 marks]

Ans: Rewrite as $(3x)^3 + y^3 + z^3 - 3(3x)(y)(z)$. By identity $a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$ with $a=3x$, $b=y$, $c=z$: $= (3x + y + z)(9x^2 + y^2 + z^2 - 3xy - yz - 3xz)$.

Section D — Long Answer

Q12. (a) Use the Factor Theorem to verify that $(x - 1)$, $(x + 2)$, and $(x - 3)$ are factors of $p(x) = x^3 - 2x^2 - 5x + 6$. (b) Hence write $p(x)$ as a product of three linear factors. [5 marks]

Ans: (a) $p(1) = 1 - 2 - 5 + 6 = 0$; $p(-2) = -8 - 8 + 10 + 6 = 0$; $p(3) = 27 - 18 - 15 + 6 = 0$. By Factor Theorem, all three are factors. (b) Since $p(x)$ is degree 3 and we have three distinct linear factors with leading coefficient 1, $p(x) = (x - 1)(x + 2)(x - 3)$.

Q13. If $a + b + c = 9$ and $ab + bc + ca = 26$, find the value of $a^2 + b^2 + c^2$. Hence find $a^3 + b^3 + c^3 - 3abc$. [4 marks]

Ans: $(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab+bc+ca)$, so $81 = a^2 + b^2 + c^2 + 52$, giving $a^2 + b^2 + c^2 = 29$. Then $a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca) = 9 \text{ times } (29 - 26) = 9 \text{ times } 3 = 27$.

★ TOPPER ANSWER TEMPLATES

5 TEMPLATES · MEMORISE THE FORMAT

★ TOPPER TEMPLATE — Factorise a cubic using the Factor Theorem

Appears as a 3-mark question in almost every CBSE Class 9 Polynomials set.

Step 1 [1 mark]	Find & verify a root	List divisors of the constant term as possible roots; test the smallest. e.g. $p(1) = 1 - 6 + 11 - 6 = 0$, so $(x - 1)$ is a factor by the Factor Theorem.
Step 2 [1 mark]	Divide out the factor	Divide the cubic by $(x - 1)$: $x^3 - 6x^2 + 11x - 6 = (x - 1)(x^2 - 5x + 6)$.
Step 3 [1 mark]	Factorise the quadratic	Split the middle term: $x^2 - 5x + 6 = (x - 2)(x - 3)$. Final answer: $(x - 1)(x - 2)(x - 3)$.

COMMON LOSS OF MARKS:

- Forgetting to write 'by Factor Theorem' as justification (-0.5)
- Not verifying the chosen root before dividing (-0.5)
- Splitting middle term incorrectly in the quadratic factor (-1)

★ TOPPER TEMPLATE — Apply the cubic identity $x^3 + y^3 + z^3 - 3xyz$

Recurrers as a 3-mark identity-application question across CBSE Class 9 papers.

Step 1 [1 mark]	State the identity	$x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)$. If $x + y + z = 0$ then $x^3 + y^3 + z^3 = 3xyz$.
Step 2 [1 mark]	Rewrite & substitute	Rewrite each cube as a base, e.g. $27x^3 + y^3 + z^3 - 9xyz = (3x)^3 + y^3 + z^3 - 3(3x)(y)(z)$, so the substitution matches the identity.
Step 3 [1 mark]	Simplify	$= (3x + y + z)(9x^2 + y^2 + z^2 - 3xy - yz - 3xz)$, keeping every cross-term sign correct.

COMMON LOSS OF MARKS:

- Writing identity with wrong signs in second bracket (-1)
- Forgetting to match $3xyz$ coefficient when rewriting (-1)
- Sign error on the cross terms $-xy, -yz, -zx$ (-0.5)

★ TOPPER TEMPLATE — Find a remainder using the Remainder Theorem

A reliable 2-mark question in CBSE Class 9 Polynomials.

Step 1 [1 mark]	Identify a & state theorem	For divisor $(x - 2)$, $a = 2$. By the Remainder Theorem the remainder equals $p(a) = p(2)$.
Step 2 [1 mark]	Substitute & simplify	$p(2) = 2^3 + 3(2^2) - 5(2) + 7 = 8 + 12 - 10 + 7 = 17$. Remainder = 17.

COMMON LOSS OF MARKS:

- Substituting $x = -2$ instead of $x = +2$ from $(x - 2)$ (-1)
- Arithmetic error in evaluating $p(a)$ (-0.5)
- Skipping the Theorem statement (-0.5)

★ TOPPER TEMPLATE — Factorise a quadratic by splitting the middle term

A standard 2-mark question in CBSE Class 9 Polynomials.

Step 1 [1 mark]	Find the split pair	For $6x^2 + 17x + 5$: need two numbers with sum $b = 17$ and product $a \cdot c = 30 \rightarrow 15$ and 2 .
Step 2 [1 mark]	Split, group & factor	$6x^2 + 15x + 2x + 5 = 3x(2x + 5) + 1(2x + 5) = (2x + 5)(3x + 1)$.

COMMON LOSS OF MARKS:

- Splitting with numbers that add but don't multiply correctly (-1)
- Sign errors when c is negative (-0.5)
- Not grouping properly leading to wrong common factor (-1)

★ TOPPER TEMPLATE — Evaluate a number using an algebraic identity

A common 2-mark question in CBSE Class 9 Polynomials.

Step 1 [1 mark]	Rewrite & state identity	$95^2 = (100-5)^2$. Use $(a-b)^2 = a^2 - 2ab + b^2$ with $a=100$, $b=5$.
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Step 2 [1 mark]	Substitute & simplify	$= 100^2 - 2(100)(5) + 5^2 = 10000 - 1000 + 25 = 9025$.
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COMMON LOSS OF MARKS:

- Using $(a+b)^2$ by mistake (-1)
- Missing the $2ab$ middle term (-1)
- Arithmetic slip in subtraction (-0.5)

MARKING SCHEME — GENERAL NOTES

- Award full marks for correct final answer with all working shown.
- Deduct half mark for missing 'by Remainder Theorem' or 'by Factor Theorem' justification when the method is the question's focus.
- In factorisation, award 1 mark for finding the first factor via Factor Theorem and 1 mark for completing the split into linear factors.
- Sign errors in the master identity ($x^3+y^3+z^3-3xyz$) cost 1 mark; a totally wrong identity costs 2 marks.
- Forgetting the $2xy$ or $3x^2y$ middle terms in squared or cubed expansions costs 1 mark per missing term.
- Arithmetic slips with otherwise correct method: deduct half mark and award method marks.
- Section D long answer: marks split as stated; partial credit per sub-step.
- No marks for unsupported one-line final answer in Section C and D.